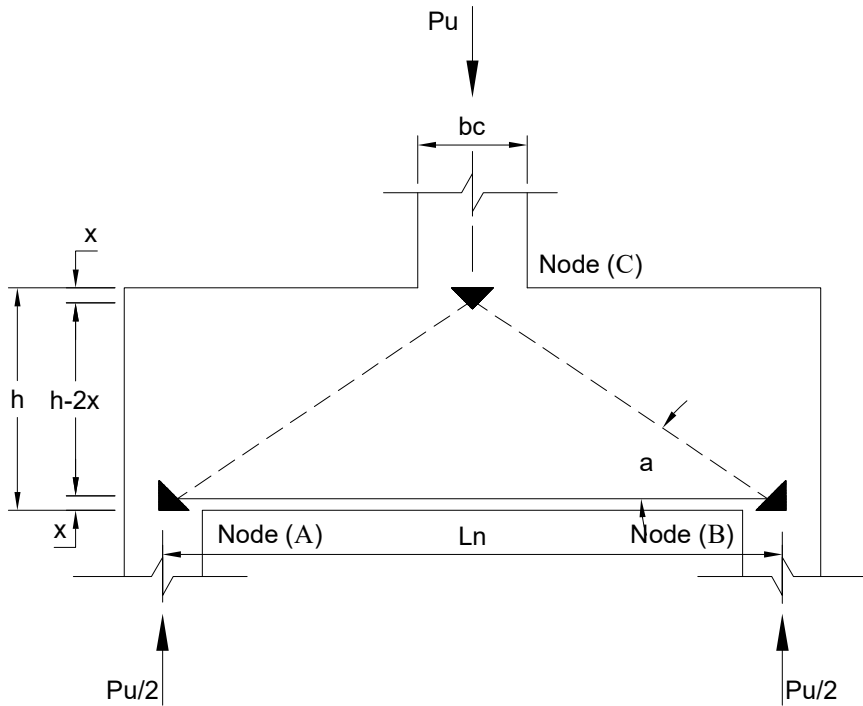




Design of Simple Span Deep Beam by the Strut-and-Tie Model as per ACI318 Appendix A



System

| | | |
|------------------------------------|----------|------------|
| Width of Deep Beam, b_c = | | 7.0 in |
| Height of Deep Beam, h = | | 60.0 in |
| Concrete Cover, co = | | 1.25 in |
| Depth of Deep Beam, d = | $h - co$ | = 58.75 in |
| End Distance of Truss Model, x = | | 5.0 in |
| Span of Deep Beam, L_n = | | 13.3 ft |
| Column Width, b_c = | | 20.0 in |

Load

| | | |
|-----------------------------------|-------------------------|--------------|
| Dead Load for Column, P_D = | | 173.35 kips |
| Live Load for Column, P_L = | | 270.0 kips |
| Service Load for Column, P = | $1.0 * P_D + 1.0 * P_L$ | = 443.4 kips |
| Ultimate Load for Column, P_u = | $1.2 * P_D + 1.6 * P_L$ | = 640.0 kips |

Material Properties

| | | |
|---|-----------------|-----------|
| Concrete Strength, f'_c = | | 4000 psi |
| Yield Strength of Reinforcement, f_y = | | 60000 psi |
| Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ = | | 0.75 |
| Modification Factor for Lightweight Concrete, λ = | | 1.00 |
| Friction Factor (According to Cl.11.6.4.3 of ACI318), μ = | $1.4 * \lambda$ | = 1.40 |

Check Deep Beam Requirements

Check on Height of Deep Beam Requirements (According to Cl.11.7.1 of ACI318),



$R = \text{IF}(12 \cdot L_n / h < 4; \text{"Deep Beam Design"}; \text{"Normal Beam Design"}) = \text{Deep Beam Design}$

Estimation of Truss Model

Length of Diagonal Strut, $L_1 = \sqrt{\left(\frac{L_n \cdot 12}{2}\right)^2 + (h - 2 \cdot x)^2} = 94.17 \text{ in}$

The Force in Diagonal Strut, $F_s = \frac{P_u}{2} \cdot \frac{L_1}{h - 2 \cdot x} = 602.69 \text{ kips}$

The Force in Horizontal Tie, $F_t = \frac{P_u}{2} \cdot \frac{0.5 \cdot L_n \cdot 12}{h - 2 \cdot x} = 510.72 \text{ kips}$

Angle Between Diagonal Strut and Horizontal Tie, $\alpha = \text{atan}\left(\frac{h - 2 \cdot x}{0.5 \cdot L_n \cdot 12}\right) = 32.07^\circ$

Check Validity (According to Cl.A.2.5 of ACI318) = $\text{IF}(\alpha > 25; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$

Calculation of Effective Concrete Strength

(According to Cl.3.2.2(a) of ACI318) Factor of, $\beta_s = 0.75$

Effective Concrete Strength (According to Eq.A-3 of ACI 318),

$f_{ce1} = 0.85 \cdot \beta_s \cdot f'_c = 2550 \text{ psi}$

Calculation of Effective Concrete Strength for Nodal Zones

For Nodal Zone C Bounded by Three Struts (C-C-C Nodal Zone)

(According to Cl.A.5.2.1 of ACI318) Factor of, $\beta_n = 1.00$

Effective Concrete Strength (According to Eq.A-3 of ACI 318),

$f_{ce2} = 0.85 \cdot \beta_n \cdot f'_c = 3400 \text{ psi}$

For Nodal Zone A&B Bounded by Three Struts (C-C-T Nodal Zone)

(According to Cl.A.5.2.2 of ACI318) Factor of, $\beta_n = 0.80$

Effective Concrete Strength (According to Eq.A-3 of ACI 318),

$f_{ce3} = 0.85 \cdot \beta_n \cdot f'_c = 2720 \text{ psi}$

Minimum Effective Concrete Strength, $f_{ce} = \text{MIN}(f_{ce1}; f_{ce2}; f_{ce3}) = 2550 \text{ psi}$

Check Strength at Node C

The Length of The Horizontal Face of Nodal Zone C,

$L_{hc} = \frac{P_u \cdot 1000}{\Phi \cdot b_c \cdot f_{ce}} = 16.73 \text{ in}$

The Length of Other Faces of Nodal Zone C,

$L_c = L_{hc} \cdot \frac{F_s}{P_u} = 15.75 \text{ in}$

Check Strength at Node A&B

The Length of The Horizontal Face of Nodal Zone A,

$L_{ha} = \frac{F_t \cdot 1000}{\Phi \cdot b_c \cdot f_{ce}} = 13.35 \text{ in}$



Width of Node at Support A,

$$La = \frac{0.5 * P_u * 1000}{\Phi * b_c * f_{ce}} = 8.37 \text{ in}$$

Calculation VL and HZ Reinforcement to Resist Splitting Diagonal Struts

1. Vertical Reinforcement

Provided Reinforcement, Bar= SEL("ACI/Bar"; Bar;) = No.4

Provided Reinforcement, A_{sbv} = TAB("ACI/Bar"; Asb; Bar=Bar) = 0.20 in²

Number of Bars, n_v = 4

Vertical Reinforcement, A_{sv} = $A_{sbv} * n_v$ = 0.80 in²

Provided Spacing between Bars, s= 11.00 in

Vertical Reinforcement (According to Eq.A4 of ACI318),

$$VL = \frac{A_{sv}}{b_c * s} * \sin(90 - \alpha) = 0.00308$$

2. Horizontal Reinforcement

Provided Reinforcement, Bar= SEL("ACI/Bar"; Bar;) = No.5

Provided Reinforcement, A_{sbh} = TAB("ACI/Bar"; Asb; Bar=Bar) = 0.31 in²

Number of Bars, n_h = 2

Vertical Reinforcement, A_{sh} = $A_{sbh} * n_h$ = 0.62 in²

Provided Spacing between Bars, s= 11.00 in

Horizontal Reinforcement (According to Eq.A4 of ACI318),

$$HZ = \frac{A_{sh}}{b_c * s} * \sin(\alpha) = 0.00150$$

Check Validity= IF(VL+HZ>0.003; "Valid"; "Invalid") = Valid

Calculation of Tension Reinforcement for Tie Connecting Node A&B

Required Reinforcement Area, A_{sreq} = $\frac{F_t * 1000}{\Phi * f_y}$ = 11.35 in²

Provided Reinforcement, Bar= SEL("ACI/Bar"; Bar;) = No.8

Provided Reinforcement, A_{sb} = TAB("ACI/Bar"; Asb; Bar=Bar) = 0.79 in²

Number of Bars, n= 16

Total Provided Area, A_{sprov} = $n * A_{sb}$ = 12.64 in²

Check Validity= IF(Asprov>Asreq; "Valid"; "Invalid") = Valid

Design Summary

Provided Vertical Reinforcement, A_{sv} = A_{sv} = 0.80 in²

Provided Horizontal Reinforcement, A_{sh} = A_{sh} = 0.62 in²

Provided Tension Reinforcement, A_{sprov} = A_{sprov} = 12.64 in²