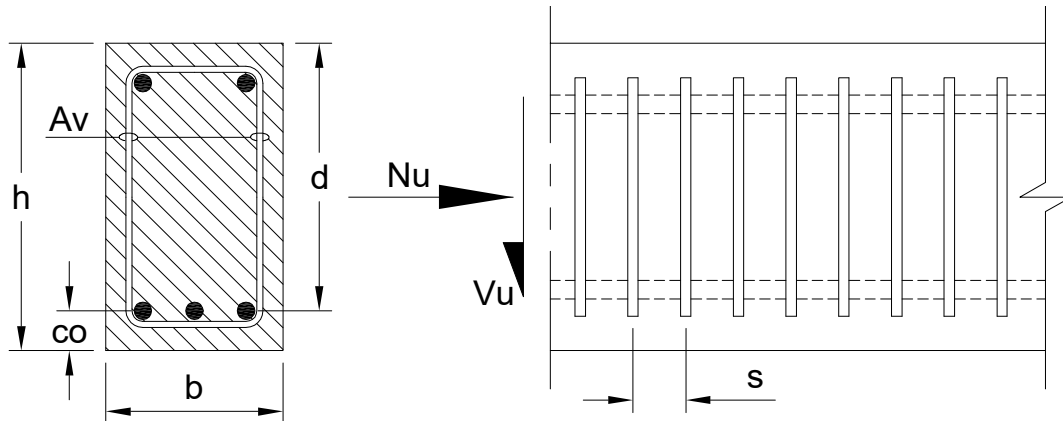




Design of Shear Reinforcement for Section Subject to Shear & Axial Compression

As per ACI318-11 Chapter 11



System

Width of Concrete Section, b=		12.0 in
Depth of Concrete Section, h=		16.0 in
Concrete Cover, co=		2.25 in
Effective Depth of Concrete Section, d=	h - co	= 13.75 in

Load

Shear Force due to Dead Load, V_D =		10.0 kips
Shear Force due to Live Load, V_L =		5.0 kips
Ultimate Shear Force, V_u =	$(1.2 * V_D) + (1.6 * V_L)$	= 20.0 kips
Axial Compression Force due to Dead Load, N_D =		4.2 kips
Axial Compression Force due to Live Load, N_L =		3.1 kips
Ultimate Axial Compression Force, N_u =	$(1.2 * N_D) + (1.6 * N_L)$	= 10.0 kips

Material Properties

Concrete Strength, f'_c =		4000 psi
Yield Strength of Reinforcement, f_y =		60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =		0.75
Modification Factor for Lightweight Concrete, λ =		1.00

Determine Concrete Shear Strength

Nominal Shear Strength provided by Concrete (According to Eq. 11-4 of ACI318),

$$V_c = 2 * \left(1 + \frac{N_u * 1000}{2000 * h * b} \right) * \lambda * \frac{\sqrt{f'_c} * b * d}{1000} = 21.4 \text{ kips}$$

Shear Reinforcement is : IF($V_u > \Phi * V_c$;"Required";"Not Required") = Required

Determine Area of Shear Reinforcement

Nominal Shear Strength provided by Reinforcement (According to Eq. 11-2 of ACI318),



$$V_s = \frac{V_u - \Phi * V_c}{\Phi} = 5.3 \text{ kips}$$

Maximum Allowable Shear Strength provided by Reinforcement (According to Cl.11.4.7.9 of ACI318),

$$V_{s_max} = 8 * \lambda * \frac{\sqrt{f'_c} * b * d}{1000} = 83.5 \text{ kips}$$

$$\text{IF}(V_s > V_{s_max}; \text{"Increase Beam Dimension"}; \text{"OK"}) = \text{OK}$$

$$\text{Spacing of Provided Stirrups, } s = 6.75 \text{ in}$$

$$\text{Required Area of Reinforcement, } A_v = \frac{V_s * s * 1000}{f_y * d} = 0.04 \text{ in}^2$$

Minimum Area of Reinforcement (According to Cl.11.4.6.3 of ACI318),

$$A_{v_min1} = \frac{0.75 * \sqrt{f'_c} * b * s}{f_y} = 0.06 \text{ in}^2$$

$$A_{v_min2} = \frac{50 * b * s}{f_y} = 0.07 \text{ in}^2$$

$$A_{v_min} = \text{MAX}(A_{v_min1}; A_{v_min2}) = 0.07 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{vc_Req} = \text{MAX}(A_v; A_{v_min}) = 0.07 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.3}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.11 \text{ in}^2$$

$$\text{Number of Stirrups, } n = 1$$

$$\text{Provided Area of Reinforcement, } A_{vc_Prov} = A_{sb} * n * 2 = 0.22 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{vc_Prov} \geq A_{vc_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Determine Maximum Permissible Spacing of Stirrups

Allowable Shear Strength provided by Reinforcement for Spacing Limit (According to Cl.11.4.5.3 of ACI318),

$$V_{s_limit} = 4 * \lambda * \sqrt{f'_c} * b * d / 1000 = 41.7 \text{ kips}$$

$$\text{Factor for Maximum Spacing of Stirrups, } Fac = \text{IF}(V_s \leq V_{s_limit}; 1; 0.5) = 1.0$$

Maximum Spacing of Stirrups (According to Cl.11.4.5.1 of ACI318),

$$s_{max} = \text{MIN}(d/2; 24) * Fac = 6.88 \text{ in}$$

$$\text{Check Validity} = \text{IF}(s \leq s_{max}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Design Summary

$$\text{Provided Area of Shear Reinforcement, } A_{vc_Prov} = A_{vc_Prov} = 0.22 \text{ in}^2$$

$$\text{Spacing of Stirrups, } s = s = 6.75 \text{ in}$$