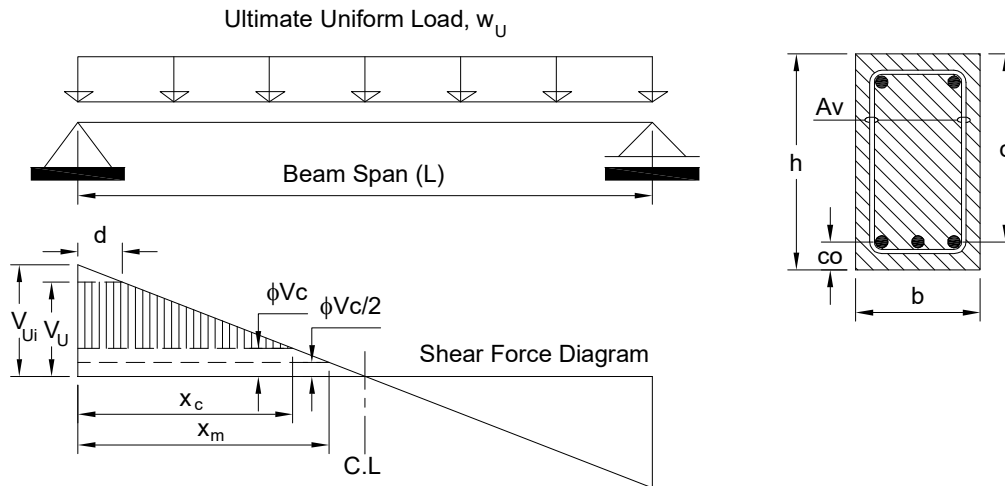




**Design of Shear Reinforcement for Section Subject to Shear & Flexure as per ACI318-11 Chapter 11**



**System**

Width of Concrete Section, \$b=\$	13.0 in
Depth of Concrete Section, \$h=\$	22.5 in
Concrete Cover, \$co=\$	2.5 in
Effective Depth of Concrete Section, \$d= h - co = 22.5 - 2.5\$	= 20.0 in
Beam Span, \$L=\$	30.0 ft

**Load**

Ultimate Uniform Load, \$w_u=\$	4.5 kip/ft
Ultimate Shear Force at Support, \$V_{ui}=\$	\$w_u * L/2 = 67.5\$ kips
Ultimate Shear Force at Distance \$[d]\$ from Support, \$V_u=V_{ui} - w_u * (d / 12)\$	= 60.0 kips

**Material Properties**

Concrete Strength, \$f'_c=\$	3000 psi
Yield Strength of Reinforcement, \$f_y=\$	40000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), \$\Phi=\$	0.75
Modification Factor for Lightweight Concrete, \$\lambda=\$	1.00
Concrete Density, \$w_c=\$	150 psi

**Determine Concrete Shear Strength**

Nominal Shear Strength provided by Concrete (According to Eq. 11-3 of ACI318),

$$V_c = 2 * \lambda * \sqrt{f'_c} * \frac{b * d}{1000} = 28.5 \text{ kips}$$

Shear Reinforcement is : IF (\$V\_u > \Phi \* V\_c\$; "Required"; "Not Required") = Required

**Determine Area of Shear Reinforcement**

Nominal Shear Strength provided by Reinforcement (According to Eq. 11-2 of ACI318),

$$V_s = \frac{V_u - \Phi * V_c}{\Phi} = 51.5 \text{ kips}$$



Maximum Allowable Shear Strength provided by Reinforcement (According to Cl.11.4.7.9 of ACI318),

$$V_{s\_max} = 8 * \sqrt{f'_c} * \frac{b * d}{1000} = 113.9 \text{ kips}$$

$$\text{IF}(V_s > V_{s\_max}; \text{"Increase Beam Dimension"}; \text{"OK"}) = \text{OK}$$

$$\text{Spacing of Provided Stirrups, } s = 6.0 \text{ in}$$

$$\text{Required Area of Reinforcement, } A_v = \frac{V_s * s * 1000}{f_y * d} = 0.39 \text{ in}^2$$

Minimum Area of Reinforcement (According to Cl.11.4.6.3 of ACI318),

$$A_{v\_min1} = \frac{0.75 * \sqrt{f'_c} * b * s}{f_y} = 0.08 \text{ in}^2$$

$$A_{v\_min2} = \frac{50 * b * s}{f_y} = 0.10 \text{ in}^2$$

$$A_{v\_min} = \text{MAX}(A_{v\_min1}; A_{v\_min2}) = 0.10 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{vc\_Req} = \text{MAX}(A_v; A_{v\_min}) = 0.39 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar}; ) = \text{No.4}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.20 \text{ in}^2$$

$$\text{Number of Stirrups, } n = 1$$

$$\text{Provided Area of Reinforcement, } A_{vc\_Prov} = A_{sb} * n * 2 = 0.40 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{vc\_Prov} \geq A_{vc\_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

#### Determine Maximum Permissible Spacing of Stirrups

Allowable Shear Strength provided by Reinforcement for Spacing Limit (According to Cl.11.4.5.3 of ACI318),

$$V_{s\_limit} = 4 * \lambda * \sqrt{f'_c} * \frac{b * d}{1000} = 57.0 \text{ kips}$$

$$\text{Factor for Maximum Spacing of Stirrups, } Fac = \text{IF}(V_s \leq V_{s\_limit}; 1; 0.5) = 1.0$$

Maximum Spacing of Stirrups (According to Cl.11.4.5.1 of ACI318),

$$s_{max} = \text{MIN}(d/2; 24) * Fac = 10.00 \text{ in}$$

$$\text{Check Validity} = \text{IF}(s \leq s_{max}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

#### Determine Distribution Distance of Shear Reinforcement

Distance from Support beyond which Minimum Shear Reinforcement is Required,

$$x_c = \frac{V_{ui} - \Phi * V_c}{W_u} = 10.3 \text{ ft}$$

Distance from Support beyond which Concrete can carry Shear Force,

$$x_m = \frac{V_{ui} - \Phi * V_c / 2}{W_u} = 12.6 \text{ ft}$$

#### Design Summary



Provided Area of Shear Reinforcement,  $A_{vc\_Prov} = A_{vc\_Prov} = 0.40 \text{ in}^2$

Distance from Support beyond which Minimum Shear Reinforcement,  $x_c = x_c = 10.3 \text{ ft}$

Distance from Support beyond which Concrete can carry Shear Force,  $x_m = x_m = 12.6 \text{ ft}$